

---

# What Is An Interval In Math

---

*What Is An Interval In Math*

Downloaded from  
[evoluir.abar.org.br](http://evoluir.abar.org.br) by  
Vazquez & Reilly

---

## INTRODUCTION

---

If you have ever worked with graphs, solved inequalities, or studied calculus, you have encountered the concept of an interval. An interval is one of the most fundamental building blocks in mathematics, especially in algebra, analysis, and geometry. It represents a continuous range of numbers between a starting point and an ending point. Understanding what an interval is and how to use it is essential for expressing solution sets, describing domains and ranges of functions, and performing operations on sets of real numbers.

In this article, we will explore the definition of an interval, the different types of intervals, how to write them using interval notation, and why they are so important in math. Whether you are a student brushing up on precalculus or someone looking to refresh your math fundamentals, this guide will give you a clear and thorough understanding of intervals.

---

## UNDERSTANDING THE CONCEPT OF AN INTERVAL

---

### Definition and Basic Notation

intervals, describing continuous ranges of numbers would be cumbersome. They provide a precise and efficient language for communicating mathematical ideas.

## TYPES OF INTERVALS

There are four main types of intervals, categorized by whether the endpoints are included and whether the interval extends to infinity.

## Closed Intervals

### $[a, b]$

A closed interval includes both endpoints. It contains every real number from  $a$  to  $b$  inclusive. Notation:  $[a, b]$ . For example,  $[0, 1]$  includes 0, 1, and every number in between. In set-builder notation:  $\{x \mid a \leq x \leq b\}$ . Closed intervals are used when the endpoints are part of the solution set, such as when an inequality has a "less than or equal to" sign.

## Open Intervals

### $(a, b)$

An open interval excludes both endpoints. It contains all numbers between  $a$  and  $b$  but not  $a$  or  $b$  themselves. Notation:  $(a, b)$ . Example:  $(0, 1)$  includes 0.5, 0.999, but not 0 or 1. Set-builder:  $\{x \mid a < x < b\}$ . Open intervals appear in strict inequalities like <

visualize intervals. Draw a horizontal line with marks for endpoints. For a closed endpoint, draw a solid dot (or filled circle). For an open endpoint, draw a hollow circle. Then shade the region between them. For infinite intervals, extend the shading with an arrow to indicate it continues forever.

For example, the interval  $[-1, 3)$  would show a solid dot at  $-1$ , a hollow circle at  $3$ , and a shaded line from  $-1$  to  $3$ . This visual representation makes it easy to see what numbers are included and helps avoid mistakes when working with unions or intersections of intervals.

---

### INTERVAL NOTATION AND SET-BUILDER NOTATION

---

Two common ways to describe sets of numbers are interval notation and set-builder notation. Interval notation is concise; set-builder is more descriptive. For the set of all numbers between  $2$  and  $5$ , inclusive of  $2$  but not  $5$ :

- **Interval notation:**  $[2, 5)$
- **Set-builder notation:**  $\{x \mid 2 \leq x < 5\}$

Learning to convert between

describe periods of motion. In statistics, confidence intervals estimate population parameters. In computer science, intervals are used in algorithms for scheduling, data analysis, and interval arithmetic.

For example, when a weather forecast

says "temperatures between 20°C and 25°C," that is an interval  $[20, 25]$ . When a company expects sales in a quarter to be between \$1 million and \$1.5 million, that is an interval. Understanding intervals helps in interpreting data ranges and making decisions based on boundaries.